## QR $\begin{aligned} & \text { Gabriel Roeder Smith \& Company } \\ & \text { Consultants \& Actuaries }\end{aligned}$

## WISCONSIN RETIREMENT SYSTEM GASB STATEMENT NO. 67 PLAN REPORTING AND ACCOUNTING SCHEDULES <br> DECEMBER 31, 2014

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July 27, 2015

Employee Trust Funds Board
Wisconsin Department of Employee
Trust Funds
801 West Badger Road
Madison, Wisconsin 53713
This report provides certain information requested by the Wisconsin Retirement System ("WRS") in connection with the Governmental Accounting Standards Board (GASB) Statement No. 67 "Accounting and Financial Reporting for Pension Plans."

The actuarial calculations in connection with this report were prepared for the purpose of complying with the requirements of GASB Statement No. 67. These calculations have been made on a basis that is consistent with our understanding of this Statement.

The calculation of the plan's liability for this report is not applicable for funding purposes of the plan. A calculation of the plan's liability for purposes other than satisfying the requirements of GASB Statement No. 67 may produce significantly different results. This report may be provided to parties other than the WRS only in its entirety and only with the permission of the WRS.

The report was based upon information, furnished by the Department of Employee Trust Funds (DETF), concerning Retirement System benefits, financial transactions, and active members, terminated members, retirees and beneficiaries. We checked for internal and year-to-year consistency, but did not otherwise audit the data. We are not responsible for the accuracy or completeness of any data provided by DETF.

This report complements the actuarial valuation report that we provided to the Board and should be considered in conjunction with that report. Please see the actuarial valuation report as of December 31, 2014 for additional discussion of the nature of actuarial calculations and more information related to participant data, economic and demographic assumptions, and benefit provisions.

This report is intended to assist in preparation of the financial statements of WRS and its participating employers. Financial statements are the responsibility of the reporting entity and not the actuary. The statements are subject to an auditor's review. Please let us know if the plan's auditor recommends any changes

Employee Trust Funds Board
Wisconsin Department of Employee
Trust Funds
July 27, 2015
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To the best of our knowledge, the information contained in this report is accurate, and fairly represents the actuarial position of WRS. All calculations have been made in conformity with generally accepted actuarial principles and practices as well as with the Actuarial Standards of Practice issued by the Actuarial Standards Board. Brian B. Murphy, Mark Buis and James D. Anderson are Members of the American Academy of Actuaries (MAAA) and meet the Qualification Standards of the Academy of Actuaries to render the actuarial opinions herein. The signing actuaries are independent of the plan sponsor.

Respectfully submitted,
Brie Br, Murphy, ASA, EA, MAAA
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## SECTION A

EXECUTIVE SUMMARY

## EXECUTIVE SUMMARY <br> AS OF DECEMBER 31, 2014

2014
December 31, 2014
December 31, 2014

185,605

- Retirees and Beneficiaries
- Inactive, Nonretired Members 154,286
- Active Members
- Total

Covered Payroll

## Net Pension Liability

Total Pension Liability
Plan Fiduciary Net Position
Net Pension Liability
Plan Fiduciary Net Position as a Percentage of Total Pension Liability
102.70\%

Net Pension Liability as a Percentage of Covered Payroll
$-18.31 \%$

Development of the Single Discount Rate
Single Discount Rate
7.20\%

Long-Term Expected Rate of Return
7.20\%

Long-Term Municipal Bond Rate 3.56\%
Last year ending December 31 in the 2015 to 2114 projection period for which projected benefit payments are fully funded

## DISCUSSION

## Accounting Standard

For pension plans that are administered through trusts or equivalent arrangements, Governmental Accounting Standards Board (GASB) Statement No. 67, "Financial Reporting for Pension Plans," replaces the requirements of GASB Statement No. 25, "Financial Reporting for Defined Benefit Pension Plans and Note Disclosures for Defined Contribution Plans," and GASB Statement No. 50, "Pension Disclosures." GASB Statement No. 67 establishes standards of financial reporting for separately issued financial reports and specifies the required approach for measuring the pension liability of employers and non-employer contributing entities for benefits provided through the pension plan.

The following discussion provides a summary of the information that is required to be disclosed under this new accounting standard. A number of these disclosure items are provided in this report. However, certain information, such as notes regarding accounting policies and investments, is not included in this report, and your internal staff will be responsible for preparing that information to comply with this accounting standard.

## Financial Statements

GASB Statement No. 67 requires defined benefit pension plans to present two financial statements - a statement of fiduciary net position and a statement of changes in fiduciary net position.

The statement of fiduciary net position presents the following items as of the end of the pension plan's reporting period, such as:

- assets;
- deferred inflows and outflows of resources;
- liabilities; and
- fiduciary net position (assets, plus deferred outflows, minus liabilities, minus deferred inflows).

The statement of changes in fiduciary net position presents the following for the plan's reporting period:

- additions, such as contributions and investment income;
- deductions, such as benefit payments and expenses; and
- net increase or decrease in the fiduciary net position (the difference between additions and deductions).


## Notes to Financial Statements

GASB Statement No. 67 also requires the notes of the plan's financial statements to include additional disclosure information. This disclosure information should include:

- a description of the types of benefits provided by the plan, as well as automatic or ad hoc COLAs;
- the number and classes of employees covered by the benefit terms;
- the composition of the pension plan's Board and the authority under which benefit terms may be amended;
- a description of the plan's funding policy, which includes member and employer contribution requirements;
- the pension plan's investment policies;
- a description of how fair value is determined;
- concentrations of investments greater than or equal to $5 \%$;
- annual money-weighted rate of return on pension plan investments;
- the portion of the present value of benefits to be provided through the pension plan to current active and inactive plan members;
- the pension plan's fiduciary net position;
- the net pension liability;
- the pension plan's fiduciary net position as a percentage of the total pension liability;
- significant assumptions and methods used to calculate the total pension liability;
- inputs to the discount rates; and
- certain information about mortality assumptions and the dates of experience studies.


## Required Supplementary Information

GASB Statement No. 67 requires a 10 -year fiscal history of:

- sources of changes in the net pension liability;
- information about the components of the net pension liability and related ratios, including the pension plan's fiduciary net position as a percentage of the total pension liability, and the net pension liability as a percent of covered-employee payroll;
- comparison of the actual employer contributions to the actuarially determined contributions based on the plan's funding policy; and
- the annual money-weighted rate of return on pension plan investments for each year.

While the first two tables may be built prospectively as the information becomes available, sufficient information is currently available for the third and fourth tables.

## Measurement of the Net Pension Liability

The net pension liability is to be measured as the total pension liability, less the amount of the pension plan's fiduciary net position. In actuarial terms, this will be the accrued liability less the market value of assets (not the smoothed actuarial value of assets that is often encountered in actuarial valuations performed to determine the employer's contribution requirement).

## Timing of the Valuation

An actuarial valuation to determine the total pension liability is required to be performed at least every two years. If the actuarial valuation is not calculated as of the plan's fiscal year end, the total pension liability is required to be rolled forward from the actuarial valuation date to the pension plan's fiscal year end.

The total pension liability shown in this report is based on an actuarial valuation performed as of December 31, 2014 and a measurement date of December 31, 2014.

## Single Discount Rate

Projected benefit payments are required to be discounted to their actuarial present values using a single discount rate that reflects (1) a long-term expected rate of return on pension plan investments (to the extent that the plan's fiduciary net position is projected to be sufficient to pay benefits) and (2) tax-exempt municipal bond rate based on an index of 20-year general obligation bonds with an average AA credit rating (which is published by the Federal Reserve) as of the measurement date (to the extent that the contributions for use with the long-term expected rate of return are not met).

For the purpose of this valuation, the expected rate of return on pension plan investments is $7.20 \%$; the municipal bond rate is $3.56 \%$ (based on the weekly rate closest to but not later than the measurement date of the 20-Year Bond Buyer Index as published by the Federal Reserve); and the resulting single discount rate is $7.20 \%$.

## Effective Date and Transition

GASB Statement No. 67 is effective for a pension plan's fiscal years beginning after June 15, 2013.

## Actuarial Assumptions and Methods and Member Census Data

The liability and asset values used in this study are taken from the December 31, 2013 and 2014 Actuarial Valuation Reports of the Wisconsin Retirement System. Therefore, the actuarial assumptions and methods employed for purposes of our Actuarial Study are the same actuarial assumptions and methods shown in the Actuarial Valuation Reports.

The member census data employed for purposes of our Actuarial Study was provided by DETF and is the same member census data used for the December 31, 2013 and December 31, 2014 Actuarial Valuation Reports of the Retirement System.

The Wisconsin Retirement System uses the Frozen Initial Liability cost method for determining funding requirements. GASB Statement No. 67 requires the use of the Entry Age Normal method for accounting purposes. Therefore, we developed the Entry Age Normal Accrued Liability to reflect the Total Pension Liability for GASB purposes.

## SECTION B

FINANCIAL STATEMENTS

# Statement of Fiduciary Net Position AS OF DECEMBER 31, 2014 

|  |  | 2014 |
| :---: | :---: | :---: |
| Assets |  |  |
| Cash and Deposits | \$ | 4,409,130,994 |
| Receivables |  |  |
| Accounts Receivable - Sale of Investments | \$ | 527,889,398 |
| Accrued Interest and Other Dividends |  | 233,038,119 |
| Contributions |  | 198,145,579 |
| Accounts Receivable - Other |  | 16,610,433 |
| Total Receivables | \$ | 975,683,529 |
| Investments |  |  |
| Fixed Income | \$ | 27,139,271,349 |
| Domestic and International Equities |  | 50,725,324,156 |
| Real Estate |  | 1,017,432,558 |
| Other |  | 14,676,108,417 |
| Total Investments | \$ | 93,558,136,480 |
| Total Assets | \$ | 98,942,951,003 |

## Liabilities

Payables
Accounts Payable - Purchase of Investments
Accrued Expenses
\$ 6,318,950,347
43,285,927
Accounts Payable - Other
Total Liabilities

Net Position Restricted for Pensions
$\$ \quad 92,147,446,988$

# Statement of Changes in Fiduciary Net Position for Year Ended December 31, 2014 

|  |  | $\mathbf{2 0 1 4}$ |
| :--- | ---: | ---: |
| Additions |  |  |
| Contributions |  |  |
| Employer | $1,023,196,702$ <br> Employee <br> Other <br> Total Contributions | $906,499,398$ |
|  |  |  |

Investment Income
Net Appreciation in Fair Value of Investments
Interest and Dividends
Less Investment Expense
Net Investment Income
Other
Total Additions

| $\$$ | $3,230,266,284$ |
| :---: | :---: |
|  | $2,020,642,457$ |
|  | $(359,218,473)$ |
| $\$$ | $4,891,690,268$ |
| $\$$ | - |
| $\$$ | $6,821,386,368$ |

## Deductions

Benefit payments, including refunds of employee contributions
Pension Plan Administrative Expense
Other Benefit Expenses
Total Deductions

Net Increase in Net Position

## Net Position Restricted for Pensions

Beginning of Year
End of Year
\$ 4,574,649,055
24,036,951
\$ 4,598,686,006
\$ 2,222,700,362

| $\$$ | $89,924,746,626$ |
| :--- | ---: |
| $\$$ | $92,147,446,988$ |

## SECTION C <br> REQUIRED SUPPLEMENTARY INFORMATION

## SCHEDULES OF REQUIRED SUPPLEMENTARY INFORMATION

## Multiyear Schedule of Changes in Net Pension Liability and Related Ratios

Fiscal year ending December 31,
Total Pension Liability
Service Cost
Interest on the Total Pension Liability
Benefit Changes
Difference between Expected and Actual Experience
Assumption Changes
Benefit Payments
Refunds
Net Change in Total Pension Liability
Total Pension Liability - Beginning
Total Pension Liability - Ending (a)
Plan Fiduciary Net Position
Employer Contributions
Employee Contributions
Pension Plan Net Investment Income

## Benefit Payments

Refunds
Pension Plan Administrative Expense Other
Net Change in Plan Fiduciary Net Position
Plan Fiduciary Net Position - Beginning
Plan Fiduciary Net Position - Ending (b)
Net Pension Liability - Ending (a) - (b)
Plan Fiduciary Net Position as a Percentage
of Total Pension Liability
Covered Employee Payroll*
Net Pension Liability as a Percentage of Covered Employee Payroll
Notes to Schedule:
N/A

* Provided by DETF.

Last 10 Fiscal Years (which may be built prospectively)

| 2014 | 2013 | 2012 | 2011 | 2010 | 2009 | 2008 | 2007 | 2006 | 2005 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| \$ 1,757,020,910 | \$ 1,745,048,505 |  |  |  |  |  |  |  |  |
| 6,089,287,273 | 5,680,664,977 |  |  |  |  |  |  |  |  |
| - | - |  |  |  |  |  |  |  |  |
| 473,101,546 | 2,659,920,220 |  |  |  |  |  |  |  |  |
| - | - |  |  |  |  |  |  |  |  |
| (4,540,247,874) | $(4,224,700,261)$ |  |  |  |  |  |  |  |  |
| (34,401,181) | (33,271,143) |  |  |  |  |  |  |  |  |
| 3,744,760,674 | 5,827,662,298 |  |  |  |  |  |  |  |  |
| 85,982,248,424 | 80,154,586,126 |  |  |  |  |  |  |  |  |
| \$ 89,727,009,098 | \$ 85,982,248,424 |  |  |  |  |  |  |  |  | 906,499398 871,259,789 4,891,690,268 11,347,296,075

$(4,540,247,874) \quad(4,224,700,261)$
$(34,401,181) \quad(33,271,143)$
(24,036,951) (22,857,502)

| $2,222,700,362$ | $8,852,425,076$ |
| :---: | :---: |
| $89,924,746,626$ | $81,072,321,550$ |
| $\$ 92,147,446,988$ | $\$ 89,924,746,626$ |
| $(2,420,437,890)$ | $(3,942,498,202)$ |
|  |  |
| $102.70 \%$ | $104.59 \%$ |
| $\$ 13,219,500,000$ | $\$$ |
|  | $12,884,800,000$ |
| $(18.31) \%$ | $(30.60) \%$ |

# SCHEDULES OF REQUIRED SUPPLEMENTARY INFORMATION Multiyear Schedule of the Net Pension Liability 

## Last 10 Fiscal Years (which may be built prospectively)

| FY Ending December 31, | Total <br> Pension Liability | Plan Net <br> Position | Net Pension Liability | Plan Net Position as a \% of Total Pension Liability | Covered <br> Payroll* | Net Pension Liability as a \% of Covered Payroll |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2005 |  |  | - |  |  |  |
| 2006 |  |  | - |  |  |  |
| 2007 |  |  | - |  |  |  |
| 2008 |  |  | - |  |  |  |
| 2009 |  |  | - |  |  |  |
| 2010 |  |  | - |  |  |  |
| 2011 |  |  | - |  |  |  |
| 2012 |  |  | - |  |  |  |
| 2013 | \$ 85,982,248,424 | \$ 89,924,746,626 | \$ (3,942,498,202) | 104.59\% | \$ 12,884,800,000 | (30.60)\% |
| 2014 | 89,727,009,098 | 92,147,446,988 | (2,420,437,890) | 102.70\% | 13,219,500,000 | (18.31)\% |

# Multiyear Schedule of Contributions 

## Last 10 Fiscal Years

| FY Ending December 31, | Actuarially <br> Determined <br> Contribution | Actual <br> Contribution | Contribution <br> Deficiency <br> (Excess) |  | Covered <br> Payroll* | Actual Contribution as a \% of Covered Payroll |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2005 |  |  |  |  |  |  |
| 2006 |  |  |  |  |  |  |
| 2007 |  |  |  |  |  |  |
| 2008 |  |  |  |  |  |  |
| 2009 |  |  |  |  |  |  |
| 2010 |  |  |  |  |  |  |
| 2011 |  |  |  |  |  |  |
| 2012 |  |  |  |  |  |  |
| 2013 | \$ 914,698,118 | \$ 914,698,118 | - | \$ | 12,884,800,000 | 7.10\% |
| 2014 | 1,023,196,702 | 1,023,196,702 | - |  | 13,219,500,000 | 7.74\% |

## Notes to Schedule of Contributions

| Valuation Date: | December 31, 2014 |
| :---: | :---: |
| Methods and Assumptions Used to Determine Actuarial Contribution on prior page: |  |
| Actuarial Cost Method | Frozen Entry Age |
| Amortization Method | Level Percentage of Payroll, Closed |
| Amortization Period | 30-Year closed from date of participation in WRS |
| Asset Valuation Method | 5-Year smoothed value |
| Inflation | $2.0 \%$ to $2.7 \%$-- approximate; No explicit price inflation assumption is used in this valuation. |
| Salary Increases | $3.2 \%$ to $8.8 \%$ including inflation |
| Net Investment Rate of Return * | 5.50\% |
| Weighted based on assumed rate for |  |
| Retired participants | 5.00\% |
| Post-retirement active participants | 5.00\% |
| Pre-retirement active participants | 7.20\% |
| Retirement Age | Experience-based table of rates that are specific to the type of eligibility condition. Last updated for the 2012 valuation pursuant to an experience study of the period 2009-2011 |
| Mortality | WRS experience projected to 2017 with scale BB |
| Other Information: |  |
| Notes | The actuarially determined contribution for calendar 2014 was determined from the December 31, 2012 actuarial valuation. |
| * For determining plan liabilities, th participants following retirement, performed assuming $5.5 \%$ discount results of an actuarial valuation using be said that the net discount rate a administrative expenses). | discount rate is $5.0 \%$ for retired participants, $5.0 \%$ for active and inactive and $7.2 \%$ for active participants prior to their retirement. A valuation rate for all participants at all stages of life, approximately reproduces the the $5.0 \%$ post-retirement and $7.2 \%$ pre-retirement assumptions. Thus, it can umed in the valuations was $5.5 \%$ per year, compounded annually (net after |

## Multiyear Schedule of Investment Returns

## Last 10 Fiscal Years



The money weighted rate of return expresses investment performance net of pension plan investment expense, adjusted for the changing amounts actually invested.

## SECTION D <br> NOTES TO FINANCIAL STATEMENTS

## Long-Term Expected Return on Plan Assets

The long-term expected rate of return on pension plan investments was determined using a building-block method in which best-estimate ranges of expected future real rates of return (expected returns, net of pension plan investment expense and inflation) are developed for each major asset class. These ranges are combined to produce the long-term expected rate of return by weighting the expected future real rates of return by the target asset allocation percentage and by adding expected inflation. The long-term expected rate of return is reviewed every three years in conjunction with the WRS experience study. For each major asset class that is included in the pension plan's target asset allocation as of December 31, 2014, these best estimates of geometric real rates of return were provided by DETF and are summarized in the following tables:

## Core Asset Allocation

| Asset Class |  |  | Long-Term Expected <br> Real Rate of Return |
| :--- | :---: | :---: | :---: |
|  |  |  |  |
| Domestic Equity |  |  |  |
| International Equity | $21.00 \%$ | $5.30 \%$ |  |
| Fixed Income | $23.00 \%$ | $5.70 \%$ |  |
| Inflation Sens. Assets | $36.00 \%$ | $1.70 \%$ |  |
| Real Estate | $20.00 \%$ | $2.30 \%$ |  |
| Private Equity/Debt | $7.00 \%$ | $4.20 \%$ |  |
| Multi-asset | $7.00 \%$ | $6.90 \%$ |  |
| Cash | $6.00 \%$ | $3.90 \%$ |  |
| Total | $-20.00 \%$ | $0.90 \%$ |  |
|  | $100.00 \%$ |  |  |

## Variable Asset Allocation

| Asset Class | Target Allocation | Long-Term Expected Real Rate of Return |
| :---: | :---: | :---: |
| Domestic Equity | 70.00\% | 5.30\% |
| International Equity | 30.00\% | 5.70\% |
| Fixed Income | N/A | N/A |
| Inflation Sens. Assets | N/A | N/A |
| Real Estate | N/A | N/A |
| Private Equity/Debt | N/A | N/A |
| Multi-asset | N/A | N/A |
| Cash | N/A | N/A |
| Total | 100.00\% |  |

## Single Discount Rate

A single discount rate of $7.20 \%$ was used to measure the total pension liability. This single discount rate was based on the expected rate of return on pension plan investments of $7.20 \%$ and a long-term bond rate of $3.56 \%$. Because of the unique structure of WRS, the $7.2 \%$ expected rate of return implies that a dividend of approximately $2.1 \%$ will always be paid. For purposes of the single discount rate, it was assumed that the dividend would always be paid. The projection of cash flows used to determine this single discount rate assumed that plan member contributions will be made at the current contribution rate and that employer contributions will be made at rates equal to the difference between actuarially determined contribution rates and the member rate. Based on these assumptions, the pension plan's fiduciary net position was projected to be available to make all projected future benefit payments (including expected dividends) of current plan members. Therefore, the long-term expected rate of return on pension plan investments was applied to all periods of projected benefit payments to determine the total pension liability.

Regarding the sensitivity of the net pension liability to changes in the single discount rate, the following presents the plan's net pension liability, calculated using a single discount rate of $7.20 \%$, as well as what the plan's net pension liability would be if it were calculated using a single discount rate that is 100 basis points lower or 100 basis points higher:

> Sensitivity of Net Pension Liability to the Single Discount Rate Assumption

|  | Current Single Discount |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{gathered} 1 \% \text { Decrease } \\ 6.20 \% \\ \hline \end{gathered}$ |  | Rate Assumption$7.20 \%$ |  | $\begin{gathered} \mathbf{1 \%} \text { Increase } \\ \mathbf{8 . 2 0 \%} \\ \hline \end{gathered}$ |  |
| Total Pension Liability | \$ | 99,168,814,841 | \$ | 89,727,009,098 | \$ | 82,303,914,056 |
| Plan Fiduciary Net Position |  | 92,147,446,988 |  | 92,147,446,988 |  | 92,147,446,988 |
| Net Pension Liability/(Asset) | \$ | 7,021,367,853 | \$ | (2,420,437,890) | \$ | (9,843,532,932) |

For the WRS, the determination of liabilities also depends on the assumed dividend which is linked to the interest rate used in the liability calculation. Therefore, we have also shown an alternative set of Sensitivity Analysis which varies the assumed dividend in conjunction with the change in the discount rate. For the liabilities shown below, the assumed dividend was $1.1 \%$ for the $6.2 \%$ discount rate, $2.1 \%$ for the $7.2 \%$ discount rate, and $3.0 \%$ for the $8.2 \%$ discount rate.

## Sensitivity of Net Pension Liability to the Single Discount Rate Assumption

|  | Current Single Discount |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{gathered} 1 \% \text { Decrease } \\ 6.20 \% \\ \hline \end{gathered}$ |  | Rate Assumption$\mathbf{7 . 2 0 \%}$ |  | $\begin{gathered} 1 \% \text { Increase } \\ 8.20 \% \\ \hline \end{gathered}$ |  |
| Total Pension Liability | \$ | 91,417,368,770 | \$ | 89,727,009,098 | \$ | 88,199,708,639 |
| Plan Fiduciary Net Position |  | 92,147,446,988 |  | 92,147,446,988 |  | 92,147,446,988 |
| Net Pension Liability/(Asset) | \$ | $(730,078,218)$ | \$ | (2,420,437,890) | \$ | (3,947,738,349) |

## Summary of Population Statistics

| Inactive Plan Members or Beneficiaries Currently Receiving Benefits | 185,605 |
| :--- | :--- |
| Inactive Plan Members Entitled to But Not Yet Receiving Benefits | 154,286 |
| Active Plan Members | 256,100 |
| Total Plan Members | 595,991 |

## SECTION E

CALCULATION OF THE SINGLE DISCOUNT RATE

## CALCULATION OF THE Single Discount Rate

GASB Statement No. 67 includes a specific requirement for the discount rate that is used for the purpose of the measurement of the Total Pension Liability. This rate considers the ability of the fund to meet benefit obligations in the future. To make this determination, employer contributions, employee contributions, benefit payments, expenses and investment returns are projected into the future. The Plan Net Position (assets) in future years can then be determined and compared to its obligation to make benefit payments in those years. As long as assets are projected to be on hand in a future year, the assumed valuation discount rate is used. In years where assets are not projected to be sufficient to meet benefit payments, the use of a "risk-free" rate is required, as described in the following paragraph.

The Single Discount Rate (SDR) is equivalent to applying these two rates to the benefits that are projected to be paid during the different time periods. The SDR reflects (1) the long-term expected rate of return on pension plan investments (during the period in which the fiduciary net position is projected to be sufficient to pay benefits) and (2) tax-exempt municipal bond rate based on an index of 20-year general obligation bonds with an average AA credit rating (which is published by the Federal Reserve) as of the measurement date (to the extent that the contributions for use with the long-term expected rate of return are not met).

For the purpose of this valuation, the expected rate of return on pension plan investments is $7.20 \%$; the municipal bond rate is $3.56 \%$; and the resulting single discount rate is $7.20 \%$.

The tables in this section provide background for the development of the single discount rate.
The Projection of Contributions table shows the development of expected contributions in future years. Normal Cost contributions for future hires are not included (nor are their liabilities).

The Projection of Plan Fiduciary Net Position table shows the development of expected asset levels in future years. Please note, that for the purposes of this projection, we have reduced the Plan Fiduciary Net Position as of December 31, 2013 to the Actuarial Accrued Liability as of December 31, 2013 (the amount of overfunding was set to zero to simplify the projection).

The Present Values of Projected Benefit Payments table shows the development of the Single Discount Rate (SDR). It breaks down the benefit payments into present values for funded and unfunded portions and shows the equivalent total at the SDR.

## Single Discount Rate Development Projection of Contributions Ending December 31, 2114

| Year | Payroll for Current Employees | Contributions from Current Employees | Normal Cost Contributions | UAL <br> Contributions | Total <br> Contributions |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | \$ 13,037,365,472 |  |  |  |  |
| 1 | 13,074,274,310 | \$ 870,576,245 | \$ 917,834,699 | \$ | \$ 1,788,410,943 |
| 2 | 12,809,047,581 | 852,871,872 | 896,364,423 | - | 1,749,236,295 |
| 3 | 12,578,508,496 | 837,481,285 | 877,466,341 | - | 1,714,947,627 |
| 4 | 12,350,886,349 | 822,284,711 | 858,668,229 | - | 1,680,952,940 |
| 5 | 12,116,103,183 | 806,614,480 | 839,265,952 | - | 1,645,880,432 |
| 6 | 11,868,355,176 | 790,084,070 | 818,917,314 | - | 1,609,001,384 |
| 7 | 11,606,743,948 | 772,634,069 | 797,644,154 | - | 1,570,278,223 |
| 8 | 11,331,674,294 | 754,289,361 | 775,511,240 | - | 1,529,800,600 |
| 9 | 11,043,649,711 | 735,082,865 | 752,544,118 | - | 1,487,626,982 |
| 10 | 10,743,304,355 | 715,060,416 | 728,846,527 | - | 1,443,906,944 |
| 11 | 10,427,721,835 | 694,026,878 | 704,258,593 | - | 1,398,285,471 |
| 12 | 10,095,403,343 | 671,880,953 | 678,751,745 | - | 1,350,632,698 |
| 13 | 9,747,694,448 | 648,711,855 | 652,416,672 | - | 1,301,128,527 |
| 14 | 9,385,968,648 | 624,614,791 | 625,377,842 | - | 1,249,992,634 |
| 15 | 9,010,603,255 | 599,612,934 | 597,644,869 | - | 1,197,257,803 |
| 16 | 8,624,047,463 | 573,868,988 | 569,448,987 | - | 1,143,317,975 |
| 17 | 8,227,972,521 | 547,495,757 | 540,874,260 | - | 1,088,370,017 |
| 18 | 7,820,623,299 | 520,373,394 | 511,806,043 | - | 1,032,179,437 |
| 19 | 7,404,115,407 | 492,642,444 | 482,363,210 | - | 975,005,655 |
| 20 | 6,980,516,253 | 464,443,826 | 452,670,524 | - | 917,114,350 |
| 21 | 6,548,009,673 | 435,655,134 | 422,604,304 | - | 858,259,438 |
| 22 | 6,107,639,460 | 406,344,146 | 392,261,691 | - | 798,605,837 |
| 23 | 5,661,570,643 | 376,657,529 | 361,813,920 | - | 738,471,449 |
| 24 | 5,210,561,197 | 346,644,365 | 331,271,424 | - | 677,915,790 |
| 25 | 4,757,389,152 | 316,489,860 | 300,824,847 | - | 617,314,707 |
| 26 | 4,306,262,595 | 286,473,556 | 270,750,718 | - | 557,224,275 |
| 27 | 3,858,219,345 | 256,662,979 | 241,120,670 | - | 497,783,649 |
| 28 | 3,411,485,817 | 226,941,698 | 211,873,786 | - | 438,815,484 |
| 29 | 2,965,444,633 | 197,267,956 | 182,986,282 | - | 380,254,238 |
| 30 | 2,525,334,375 | 167,989,989 | 154,789,295 | - | 322,779,284 |
| 31 | 2,108,577,608 | 140,266,585 | 128,386,389 | - | 268,652,974 |
| 32 | 1,730,717,970 | 115,130,280 | 104,723,520 | - | 219,853,800 |
| 33 | 1,397,535,204 | 92,966,339 | 84,084,185 | - | 177,050,524 |
| 34 | 1,113,280,387 | 74,058,105 | 66,639,791 | - | 140,697,896 |
| 35 | 877,855,958 | 58,396,931 | 52,303,670 | - | 110,700,601 |
| 36 | 687,321,872 | 45,721,698 | 40,773,915 | - | 86,495,614 |
| 37 | 534,366,125 | 35,547,288 | 31,567,421 | - | 67,114,709 |
| 38 | 411,902,687 | 27,400,825 | 24,235,589 | - | 51,636,414 |
| 39 | 315,157,150 | 20,965,160 | 18,463,379 | - | 39,428,539 |
| 40 | 239,718,609 | 15,946,843 | 13,982,986 | - | 29,929,829 |
| 41 | 181,175,032 | 12,052,248 | 10,508,827 | - | 22,561,075 |
| 42 | 136,087,234 | 9,053,019 | 7,841,102 | - | 16,894,121 |
| 43 | 101,727,072 | 6,767,369 | 5,816,445 | - | 12,583,814 |
| 44 | 75,714,774 | 5,036,840 | 4,291,155 | - | 9,327,995 |
| 45 | 55,935,044 | 3,720,906 | 3,135,930 | - | 6,856,836 |
| 46 | 40,635,310 | 2,703,059 | 2,250,336 | - | 4,953,395 |
| 47 | 28,880,474 | 1,921,095 | 1,575,009 | - | 3,496,104 |
| 48 | 20,044,007 | 1,333,264 | 1,075,844 | - | 2,409,108 |
| 49 | 13,360,499 | 888,634 | 706,012 | - | 1,594,646 |
| 50 | 8,309,889 | 552,668 | 431,988 | - | 984,656 |

# Single Discount Rate Development Projection of Contributions Ending December 31, 2114 (CONCLUDED) 

| Year | Payroll for Current Employees | Contributions from Current Employees | Normal Cost Contributions | UAL <br> Contributions | Total <br> Contributions |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 51 | \$ 4,619,345 | \$ 307,186 | \$ 235,372 | \$ | \$ 542,558 |
| 52 | 2,227,710 | 148,143 | 110,403 | - | 258,546 |
| 53 | 966,204 | 64,253 | 46,468 | - | 110,721 |
| 54 | 427,359 | 28,419 | 20,126 | - | 48,545 |
| 55 | 181,174 | 12,048 | 8,530 | - | 20,578 |
| 56 | 55,084 | 3,663 | 2,567 | - | 6,230 |
| 57 | 10,733 | 714 | 510 | - | 1,224 |
| 58 | 1,139 | 76 | 54 | - | 130 |
| 59 | 338 | 22 | 19 | - | 41 |
| 60 | - | - | - | - | - |
| 61 | - | - | - | - | - |
| 62 | - | - | - | - | - |
| 63 | - | - | - | - | - |
| 64 | - | - | - | - | - |
| 65 | - | - | - | - | - |
| 66 | - | - | - | - | - |
| 67 | - | - | - | - | - |
| 68 | - | - | - | - | - |
| 69 | - | - | - | - | - |
| 70 | - | - | - | - | - |
| 71 | - | - | - | - | - |
| 72 | - | - | - | - | - |
| 73 | - | - | - | - | - |
| 74 | - | - | - | - | - |
| 75 | - | - | - | - | - |
| 76 | - | - | - | - | - |
| 77 | - | - | - | - | - |
| 78 | - | - | - | - | - |
| 79 | - | - | - | - | - |
| 80 | - | - | - | - | - |
| 81 | - | - | - | - | - |
| 82 | - | - | - | - | - |
| 83 | - | - | - | - | - |
| 84 | - | - | - | - | - |
| 85 | - | - | - | - | - |
| 86 | - | - | - | - | - |
| 87 | - | - | - | - | - |
| 88 | - | - | - | - | - |
| 89 | - | - | - | - | - |
| 90 | - | - | - | - | - |
| 91 | - | - | - | - | - |
| 92 | - | - | - | - | - |
| 93 | - | - | - | - | - |
| 94 | - | - | - | - | - |
| 95 | - | - | - | - | - |
| 96 | - | - | - | - | - |
| 97 | - | - | - | - | - |
| 98 | - | - | - | - | - |
| 99 | - | - | - | - | - |
| 100 | - | - | - | - | - |

## Single Discount Rate Development Projection of Plan Fiduciary Net Position Ending DECEMBER 31, 2114

| Year | Projected Beginning Plan Net Position* | Projected Total Contributions | Projected Benefit Payments Including Dividends | Projected Investment Earnings at $7.20 \%$ | Projected Ending Plan <br> Net Position |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | (a) | (b) | (c) | (d) | (e) $=(\mathrm{a})+(\mathrm{b})$-(c) + (d) |
| 1 | 89,727,009,098 | \$ 1,788,410,943 | \$ 4,809,585,044 | \$ 6,353,472,650 | \$ 93,059,307,647 |
| 2 | 93,059,307,647 | 1,749,236,295 | 5,002,787,604 | 6,585,177,958 | 96,390,934,297 |
| 3 | 96,390,934,297 | 1,714,947,627 | 5,205,528,291 | 6,816,670,322 | 99,717,023,955 |
| 4 | 99,717,023,955 | 1,680,952,940 | 5,421,402,350 | 7,047,309,839 | 103,023,884,383 |
| 5 | 103,023,884,383 | 1,645,880,432 | 5,655,039,690 | 7,275,898,359 | 106,290,623,485 |
| 6 | 106,290,623,485 | 1,609,001,384 | 5,910,602,815 | 7,500,758,629 | 109,489,780,682 |
| 7 | 109,489,780,682 | 1,570,278,223 | 6,182,182,760 | 7,720,121,183 | 112,597,997,328 |
| 8 | 112,597,997,328 | 1,529,800,600 | 6,466,665,452 | 7,932,417,529 | 115,593,550,006 |
| 9 | 115,593,550,006 | 1,487,626,982 | 6,760,784,894 | 8,136,201,181 | 118,456,593,275 |
| 10 | 118,456,593,275 | 1,443,906,944 | 7,059,764,803 | 8,330,217,515 | 121,170,952,931 |
| 11 | 121,170,952,931 | 1,398,285,471 | 7,371,641,177 | 8,513,005,164 | 123,710,602,389 |
| 12 | 123,710,602,389 | 1,350,632,698 | 7,681,303,233 | 8,683,220,153 | 126,063,152,007 |
| 13 | 126,063,152,007 | 1,301,128,527 | 7,988,694,831 | 8,839,978,778 | 128,215,564,482 |
| 14 | 128,215,564,482 | 1,249,992,634 | 8,293,025,295 | 8,982,378,092 | 130,154,909,912 |
| 15 | 130,154,909,912 | 1,197,257,803 | 8,589,870,720 | 9,109,644,796 | 131,871,941,792 |
| 16 | 131,871,941,792 | 1,143,317,975 | 8,883,950,935 | 9,220,960,116 | 133,352,268,948 |
| 17 | 133,352,268,948 | 1,088,370,017 | 9,173,561,808 | 9,315,355,134 | 134,582,432,291 |
| 18 | 134,582,432,291 | 1,032,179,437 | 9,452,990,615 | 9,392,054,585 | 135,553,675,698 |
| 19 | 135,553,675,698 | 975,005,655 | 9,720,859,800 | 9,450,485,933 | 136,258,307,485 |
| 20 | 136,258,307,485 | 917,114,350 | 9,976,345,589 | 9,490,133,918 | 136,689,210,165 |
| 21 | 136,689,210,165 | 858,259,438 | 10,219,833,298 | 9,510,463,743 | 136,838,100,049 |
| 22 | 136,838,100,049 | 798,605,837 | 10,449,006,994 | 9,510,966,743 | 136,698,665,635 |
| 23 | 136,698,665,635 | 738,471,449 | 10,657,592,081 | 9,491,421,695 | 136,270,966,697 |
| 24 | 136,270,966,697 | 677,915,790 | 10,846,242,125 | 9,451,811,887 | 135,554,452,249 |
| 25 | 135,554,452,249 | 617,314,707 | 11,019,002,629 | 9,391,967,837 | 134,544,732,164 |
| 26 | 134,544,732,164 | 557,224,275 | 11,174,303,676 | 9,311,648,662 | 133,239,301,425 |
| 27 | 133,239,301,425 | 497,783,649 | 11,309,400,207 | 9,210,776,027 | 131,638,460,895 |
| 28 | 131,638,460,895 | 438,815,484 | 11,428,589,927 | 9,089,213,294 | 129,737,899,745 |
| 29 | 129,737,899,745 | 380,254,238 | 11,533,093,544 | 8,946,604,581 | 127,531,665,021 |
| 30 | 127,531,665,021 | 322,779,284 | 11,620,448,470 | 8,782,632,421 | 125,016,628,256 |
| 31 | 125,016,628,256 | 268,652,974 | 11,684,337,536 | 8,597,375,059 | 122,198,318,752 |
| 32 | 122,198,318,752 | 219,853,800 | 11,715,534,673 | 8,391,626,959 | 119,094,264,838 |
| 33 | 119,094,264,838 | 177,050,524 | 11,709,980,163 | 8,166,817,427 | 115,728,152,626 |
| 34 | 115,728,152,626 | 140,697,896 | 11,664,475,979 | 7,924,781,078 | 112,129,155,622 |
| 35 | 112,129,155,622 | 110,700,601 | 11,581,343,815 | 7,667,532,904 | 108,326,045,312 |
| 36 | 108,326,045,312 | 86,495,614 | 11,464,334,104 | 7,396,991,867 | 104,345,198,688 |
| 37 | 104,345,198,688 | 67,114,709 | 11,314,205,442 | 7,114,996,024 | 100,213,103,979 |
| 38 | 100,213,103,979 | 51,636,414 | 11,134,031,068 | 6,823,311,218 | 95,954,020,544 |
| 39 | 95,954,020,544 | 39,428,539 | 10,926,719,543 | 6,523,558,871 | 91,590,288,411 |
| 40 | 91,590,288,411 | 29,929,829 | 10,692,933,947 | 6,217,304,156 | 87,144,588,449 |
| 41 | 87,144,588,449 | 22,561,075 | 10,432,449,551 | 5,906,167,554 | 82,640,867,527 |
| 42 | 82,640,867,527 | 16,894,121 | 10,143,144,673 | 5,591,933,149 | 78,106,550,124 |
| 43 | 78,106,550,124 | 12,583,814 | 9,825,341,724 | 5,276,551,888 | 73,570,344,102 |
| 44 | 73,570,344,102 | 9,327,995 | 9,484,087,097 | 4,961,901,535 | 69,057,486,535 |
| 45 | 69,057,486,535 | 6,856,836 | 9,126,378,690 | 4,649,542,069 | 64,587,506,751 |
| 46 | 64,587,506,751 | 4,953,395 | 8,755,994,885 | 4,340,738,270 | 60,177,203,530 |
| 47 | 60,177,203,530 | 3,496,104 | 8,374,189,349 | 4,036,651,002 | 55,843,161,287 |
| 48 | 55,843,161,287 | 2,409,108 | 7,982,497,999 | 3,738,417,327 | 51,601,489,723 |
| 49 | 51,601,489,723 | 1,594,646 | 7,582,774,647 | 3,447,128,109 | 47,467,437,831 |
| 50 | 47,467,437,831 | 984,656 | 7,176,485,860 | 3,163,826,988 | 43,455,763,615 |

* For the purposes of this projection, the amount of overfunding as of December 31, 2014 was ignored.


# Single Discount Rate Development Projection of Plan Fiduciary Net Position Ending DECEMBER 31, 2114 (CONCLUDED) 

| Year |  | ojected Beginning <br> Plan Net Position |  | Projected Total Contributions |  | ojected Benefit <br> Payments <br> Including <br> Dividends |  | Projected Investment Earnings at $\mathbf{7 . 2 0 \%}$ |  | Projected Ending Plan <br> Net Position |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | (a) |  | (b) |  | (c) |  | (d) |  | (e) $=$ (a)+(b)-(c)+(d) |
| 51 | \$ | 43,455,763,615 | \$ | 542,558 | \$ | 6,764,907,380 |  | \$ 2,889,530,117 | \$ | 39,580,928,911 |
| 52 |  | 39,580,928,911 |  | 258,546 |  | 6,349,299,561 |  | 2,625,233,819 |  | 35,857,121,715 |
| 53 |  | 35,857,121,715 |  | 110,721 |  | 5,931,388,771 |  | 2,371,897,786 |  | 32,297,741,450 |
| 54 |  | 32,297,741,450 |  | 48,545 |  | 5,513,572,170 |  | 2,130,400,189 |  | 28,914,618,014 |
| 55 |  | 28,914,618,014 |  | 20,578 |  | 5,098,433,311 |  | 1,901,499,570 |  | 25,717,704,852 |
| 56 |  | 25,717,704,852 |  | 6,230 |  | 4,688,118,307 |  | 1,685,835,933 |  | 22,715,428,707 |
| 57 |  | 22,715,428,707 |  | 1,224 |  | 4,284,577,475 |  | 1,483,946,859 |  | 19,914,799,315 |
| 58 |  | 19,914,799,315 |  | 130 |  | 3,889,889,379 |  | 1,296,263,331 |  | 17,321,173,397 |
| 59 |  | 17,321,173,397 |  | 41 |  | 3,506,220,540 |  | 1,123,094,289 |  | 14,938,047,187 |
| 60 |  | 14,938,047,187 |  | - |  | 3,135,816,923 |  | 964,611,980 |  | 12,766,842,243 |
| 61 |  | 12,766,842,243 |  | - |  | 2,780,970,556 |  | 820,837,676 |  | 10,806,709,363 |
| 62 |  | 10,806,709,363 |  | - |  | 2,443,967,874 |  | 691,629,352 |  | 9,054,370,841 |
| 63 |  | 9,054,370,841 |  | - |  | 2,126,985,330 |  | 576,674,023 |  | 7,504,059,534 |
| 64 |  | 7,504,059,534 |  | - |  | 1,831,942,919 |  | 475,488,536 |  | 6,147,605,150 |
| 65 |  | 6,147,605,150 |  | - |  | 1,560,364,078 |  | 387,430,739 |  | 4,974,671,812 |
| 66 |  | 4,974,671,812 |  | - |  | 1,313,262,830 |  | 311,720,580 |  | 3,973,129,562 |
| 67 |  | 3,973,129,562 |  | - |  | 1,091,104,363 |  | 247,468,244 |  | 3,129,493,443 |
| 68 |  | 3,129,493,443 |  | - |  | 893,888,311 |  | 193,702,829 |  | 2,429,307,960 |
| 69 |  | 2,429,307,960 |  | - |  | 721,239,514 |  | 149,396,810 |  | 1,857,465,256 |
| 70 |  | 1,857,465,256 |  | - |  | 572,437,828 |  | 113,487,895 |  | 1,398,515,323 |
| 71 |  | 1,398,515,323 |  | - |  | 446,441,063 |  | 84,900,550 |  | 1,036,974,811 |
| 72 |  | 1,036,974,811 |  | - |  | 341,896,120 |  | 62,567,841 |  | 757,646,531 |
| 73 |  | 757,646,531 |  | - |  | 257,107,054 |  | 45,455,561 |  | 545,995,038 |
| 74 |  | 545,995,038 |  | - |  | 190,006,888 |  | 32,590,277 |  | 388,578,427 |
| 75 |  | 388,578,427 |  | - |  | 138,204,326 |  | 23,088,762 |  | 273,462,862 |
| 76 |  | 273,462,862 |  | - |  | 99,125,252 |  | 16,182,837 |  | 190,520,447 |
| 77 |  | 190,520,447 |  | - |  | 70,233,001 |  | 11,233,027 |  | 131,520,473 |
| 78 |  | 131,520,473 |  | - |  | 49,234,316 |  | 7,727,843 |  | 90,014,001 |
| 79 |  | 90,014,001 |  | - |  | 34,189,353 |  | 5,271,583 |  | 61,096,230 |
| 80 |  | 61,096,230 |  | - |  | 23,536,724 |  | 3,566,333 |  | 41,125,839 |
| 81 |  | 41,125,839 |  | - |  | 16,069,379 |  | 2,392,617 |  | 27,449,076 |
| 82 |  | 27,449,076 |  | - |  | 10,882,277 |  | 1,591,380 |  | 18,158,179 |
| 83 |  | 18,158,179 |  | - |  | 7,309,272 |  | 1,048,828 |  | 11,897,735 |
| 84 |  | 11,897,735 |  | - |  | 4,867,279 |  | 684,460 |  | 7,714,917 |
| 85 |  | 7,714,917 |  | - |  | 3,210,908 |  | 441,890 |  | 4,945,899 |
| 86 |  | 4,945,899 |  | - |  | 2,096,158 |  | 281,955 |  | 3,131,696 |
| 87 |  | 3,131,696 |  | - |  | 1,352,679 |  | 177,632 |  | 1,956,649 |
| 88 |  | 1,956,649 |  | - |  | 862,092 |  | 110,383 |  | 1,204,939 |
| 89 |  | 1,204,939 |  | - |  | 542,449 |  | 67,567 |  | 730,058 |
| 90 |  | 730,058 |  | - |  | 336,874 |  | 40,647 |  | 433,831 |
| 91 |  | 433,831 |  | - |  | 206,136 |  | 23,944 |  | 251,639 |
| 92 |  | 251,639 |  | - |  | 124,034 |  | 13,730 |  | 141,335 |
| 93 |  | 141,335 |  | - |  | 73,031 |  | 7,593 |  | 75,897 |
| 94 |  | 75,897 |  | - |  | 41,606 |  | 3,993 |  | 38,283 |
| 95 |  | 38,283 |  | - |  | 22,456 |  | 1,962 |  | 17,790 |
| 96 |  | 17,790 |  | - |  | 11,125 |  | 887 |  | 7,552 |
| 97 |  | 7,552 |  | - |  | 4,918 |  | 370 |  | 3,004 |
| 98 |  | 3,004 |  | - |  | 1,981 |  | 146 |  | 1,168 |
| 99 |  | 1,168 |  | - |  | 807 |  | 56 |  | 417 |
| 100 |  | 417 |  | - |  | 432 |  | 15 |  | - |

# Single Discount Rate Development Present Values of Projected Benefits 

ENDING DECEMBER 31, 2114

| Year | Projected Beginning Plan Net Position | Projected Benefit Payments | Funded Portion of Benefit Payments | Unfunded Portion of Benefit Payments | Present Value of Funded Benefit Payments using Expected Return Rate (v) | Present Value of Unfunded Benefit Payments using Municipal Bond Rate (vf) | Present Value of Benefit <br> Payments using Single Discount Rate (sdr) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (a) | (b) | (c) | (d) | (e) | $(\mathrm{f})=(\mathrm{d}) * \mathrm{v}^{\wedge}((\mathrm{a})-.5)$ | $(\mathrm{g})=(\mathrm{e}) * \mathrm{vf} \wedge((\mathrm{a})-.5)$ | $(\mathrm{h})=\left((\mathrm{c}) /(1+\mathrm{sdr})^{\wedge}(\mathrm{a}-.5)\right.$ |
| 1 | \$ 89,727,009,098 | \$ 4,809,585,044 | \$ 4,809,585,044 | \$ | \$ 4,645,262,020 | \$ | \$ 4,645,262,020 |
| 2 | 93,059,307,647 | 5,002,787,604 | 5,002,787,604 | - | 4,507,335,514 | - | 4,507,335,514 |
| 3 | 96,390,934,297 | 5,205,528,291 | 5,205,528,291 | - | 4,374,997,888 | - | 4,374,997,888 |
| 4 | 99,717,023,955 | 5,421,402,350 | 5,421,402,350 | - | 4,250,400,862 | - | 4,250,400,862 |
| 5 | 103,023,884,383 | 5,655,039,690 | 5,655,039,690 | - | 4,135,796,137 | - | 4,135,796,137 |
| 6 | 106,290,623,485 | 5,910,602,815 | 5,910,602,815 | - | 4,032,370,760 | - | 4,032,370,760 |
| 7 | 109,489,780,682 | 6,182,182,760 | 6,182,182,760 | - | 3,934,374,847 | - | 3,934,374,847 |
| 8 | 112,597,997,328 | 6,466,665,452 | 6,466,665,452 | - | 3,839,012,299 | - | 3,839,012,299 |
| 9 | 115,593,550,006 | 6,760,784,894 | 6,760,784,894 | - | 3,744,048,301 | - | 3,744,048,301 |
| 10 | 118,456,593,275 | 7,059,764,803 | 7,059,764,803 | - | 3,647,033,662 | - | 3,647,033,662 |
| 11 | 121,170,952,931 | 7,371,641,177 | 7,371,641,177 | - | 3,552,376,113 | - | 3,552,376,113 |
| 12 | 123,710,602,389 | 7,681,303,233 | 7,681,303,233 | - | 3,452,986,484 | - | 3,452,986,484 |
| 13 | 126,063,152,007 | 7,988,694,831 | 7,988,694,831 | - | 3,349,970,745 | - | 3,349,970,745 |
| 14 | 128,215,564,482 | 8,293,025,295 | 8,293,025,295 | - | 3,244,018,989 | - | 3,244,018,989 |
| 15 | 130,154,909,912 | 8,589,870,720 | 8,589,870,720 | - | 3,134,456,448 | - | 3,134,456,448 |
| 16 | 131,871,941,792 | 8,883,950,935 | 8,883,950,935 | - | 3,024,036,149 | - | 3,024,036,149 |
| 17 | 133,352,268,948 | 9,173,561,808 | 9,173,561,808 | - | 2,912,889,654 | - | 2,912,889,654 |
| 18 | 134,582,432,291 | 9,452,990,615 | 9,452,990,615 | - | 2,800,015,806 | - | 2,800,015,806 |
| 19 | 135,553,675,698 | 9,720,859,800 | 9,720,859,800 | - | 2,685,969,955 | - | 2,685,969,955 |
| 20 | 136,258,307,485 | 9,976,345,589 | 9,976,345,589 | - | 2,571,420,907 | - | 2,571,420,907 |
| 21 | 136,689,210,165 | 10,219,833,298 | 10,219,833,298 | - | 2,457,257,742 | - | 2,457,257,742 |
| 22 | 136,838,100,049 | 10,449,006,994 | 10,449,006,994 | - | 2,343,619,672 | - | 2,343,619,672 |
| 23 | 136,698,665,635 | 10,657,592,081 | 10,657,592,081 | - | 2,229,853,972 | - | 2,229,853,972 |
| 24 | 136,270,966,697 | 10,846,242,125 | 10,846,242,125 | - | 2,116,907,294 | - | 2,116,907,294 |
| 25 | 135,554,452,249 | 11,019,002,629 | 11,019,002,629 | - | 2,006,180,688 | - | 2,006,180,688 |
| 26 | 134,544,732,164 | 11,174,303,676 | 11,174,303,676 | - | 1,897,813,113 | - | 1,897,813,113 |
| 27 | 133,239,301,425 | 11,309,400,207 | 11,309,400,207 | - | 1,791,751,434 | - | 1,791,751,434 |
| 28 | 131,638,460,895 | 11,428,589,927 | 11,428,589,927 | - | 1,689,024,902 | - | 1,689,024,902 |
| 29 | 129,737,899,745 | 11,533,093,544 | 11,533,093,544 | - | 1,589,990,143 | - | 1,589,990,143 |
| 30 | 127,531,665,021 | 11,620,448,470 | 11,620,448,470 | - | 1,494,433,936 | - | 1,494,433,936 |
| 31 | 125,016,628,256 | 11,684,337,536 | 11,684,337,536 | - | 1,401,726,039 | - | 1,401,726,039 |
| 32 | 122,198,318,752 | 11,715,534,673 | 11,715,534,673 | - | 1,311,071,494 | - | 1,311,071,494 |
| 33 | 119,094,264,838 | 11,709,980,163 | 11,709,980,163 | - | 1,222,434,604 | - | 1,222,434,604 |
| 34 | 115,728,152,626 | 11,664,475,979 | 11,664,475,979 | - | 1,135,899,540 | - | 1,135,899,540 |
| 35 | 112,129,155,622 | 11,581,343,815 | 11,581,343,815 | - | 1,052,056,006 | - | 1,052,056,006 |
| 36 | 108,326,045,312 | 11,464,334,104 | 11,464,334,104 | - | 971,480,201 | - | 971,480,201 |
| 37 | 104,345,198,688 | 11,314,205,442 | 11,314,205,442 | - | 894,364,175 | - | 894,364,175 |
| 38 | 100,213,103,979 | 11,134,031,068 | 11,134,031,068 | - | 821,009,113 | - | 821,009,113 |
| 39 | 95,954,020,544 | 10,926,719,543 | 10,926,719,543 | - | 751,606,556 | - | 751,606,556 |
| 40 | 91,590,288,411 | 10,692,933,947 | 10,692,933,947 | - | 686,124,398 | - | 686,124,398 |
| 41 | 87,144,588,449 | 10,432,449,551 | 10,432,449,551 | - | 624,449,736 | - | 624,449,736 |
| 42 | 82,640,867,527 | 10,143,144,673 | 10,143,144,673 | - | 566,355,376 | - | 566,355,376 |
| 43 | 78,106,550,124 | 9,825,341,724 | 9,825,341,724 | - | 511,763,475 | - | 511,763,475 |
| 44 | 73,570,344,102 | 9,484,087,097 | 9,484,087,097 | - | 460,810,505 | - | 460,810,505 |
| 45 | 69,057,486,535 | 9,126,378,690 | 9,126,378,690 | - | 413,647,627 | - | 413,647,627 |
| 46 | 64,587,506,751 | 8,755,994,885 | 8,755,994,885 | - | 370,205,414 | - | 370,205,414 |
| 47 | 60,177,203,530 | 8,374,189,349 | 8,374,189,349 | - | 330,282,267 | - | 330,282,267 |
| 48 | 55,843,161,287 | 7,982,497,999 | 7,982,497,999 | - | 293,688,211 | - | 293,688,211 |
| 49 | 51,601,489,723 | 7,582,774,647 | 7,582,774,647 | - | 260,244,200 | - | 260,244,200 |
| 50 | 47,467,437,831 | 7,176,485,860 | 7,176,485,860 | - | 229,757,638 | - | 229,757,638 |

* For the purposes of this projection, the amount of overfunding as of December 31, 2014 was ignored.


# Single Discount Rate Development <br> Present Values of Projected Benefits Ending December 31, 2114 (CONTINUED) 

| Year |  | Projected eginning Plan Net Position |  | rojected Benefit Payments |  | ded Portion of nefit Payments |  | Unfunded Portion of Benefit Payments | Present Value of Funded Benefit Payments using Expected Return Rate (v) | Present Value of Unfunded Benefit Payments using Municipal Bond Rate (vf) | Present Value of Benefit Payments using Single Discount Rate (sdr) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (a) |  | (b) |  | (c) |  | (d) |  | (e) | (f)=(d)*v^((a)-.5) | (g)=(e)*vf^((a).-5) | (h) $=\left((\mathrm{c})(1+\mathrm{sdr})^{\wedge}(\mathrm{a}-.5)\right.$ |
| 51 | \$ | 43,455,763,615 | \$ | 6,764,907,380 | \$ | 6,764,907,380 | \$ | - | \$ 202,034,341 | \$ | 202,034,341 |
| 52 |  | 39,580,928,911 |  | 6,349,299,561 |  | 6,349,299,561 |  | - | 176,886,371 | - | 176,886,371 |
| 53 |  | 35,857,121,715 |  | 5,931,388,771 |  | 5,931,388,771 |  | - | 154,145,255 | - | 154,145,255 |
| 54 |  | 32,297,741,450 |  | 5,513,572,170 |  | 5,513,572,170 |  | - | 133,663,259 | - | 133,663,259 |
| 55 |  | 28,914,618,014 |  | 5,098,433,311 |  | 5,098,433,311 |  | - | 115,297,779 | - | 115,297,779 |
| 56 |  | 25,717,704,852 |  | 4,688,118,307 |  | 4,688,118,307 |  | - | 98,898,106 | - | 98,898,106 |
| 57 |  | 22,715,428,707 |  | 4,284,577,475 |  | 4,284,577,475 |  | - | 84,314,570 | - | 84,314,570 |
| 58 |  | 19,914,799,315 |  | 3,889,889,379 |  | 3,889,889,379 |  | - | 71,406,393 | - | 71,406,393 |
| 59 |  | 17,321,173,397 |  | 3,506,220,540 |  | 3,506,220,540 |  | - | 60,040,498 | - | 60,040,498 |
| 60 |  | 14,938,047,187 |  | 3,135,816,923 |  | 3,135,816,923 |  | - | 50,091,146 | - | 50,091,146 |
| 61 |  | 12,766,842,243 |  | 2,780,970,556 |  | 2,780,970,556 |  | - | 41,439,249 | - | 41,439,249 |
| 62 |  | 10,806,709,363 |  | 2,443,967,874 |  | 2,443,967,874 |  | - | 33,971,615 | - | 33,971,615 |
| 63 |  | 9,054,370,841 |  | 2,126,985,330 |  | 2,126,985,330 |  | - | 27,579,755 | - | 27,579,755 |
| 64 |  | 7,504,059,534 |  | 1,831,942,919 |  | 1,831,942,919 |  | - | 22,158,638 | - | 22,158,638 |
| 65 |  | 6,147,605,150 |  | 1,560,364,078 |  | 1,560,364,078 |  | - | 17,606,064 | - | 17,606,064 |
| 66 |  | 4,974,671,812 |  | 1,313,262,830 |  | 1,313,262,830 |  | - | 13,822,710 | - | 13,822,710 |
| 67 |  | 3,973,129,562 |  | 1,091,104,363 |  | 1,091,104,363 |  | - | 10,713,048 | - | 10,713,048 |
| 68 |  | 3,129,493,443 |  | 893,888,311 |  | 893,888,311 |  | - | 8,187,197 | - | 8,187,197 |
| 69 |  | 2,429,307,960 |  | 721,239,514 |  | 721,239,514 |  | - | 6,162,213 | - | 6,162,213 |
| 70 |  | 1,857,465,256 |  | 572,437,828 |  | 572,437,828 |  | - | 4,562,373 | - | 4,562,373 |
| 71 |  | 1,398,515,323 |  | 446,441,063 |  | 446,441,063 |  | - | 3,319,187 | - | 3,319,187 |
| 72 |  | 1,036,974,811 |  | 341,896,120 |  | 341,896,120 |  | - | 2,371,194 | - | 2,371,194 |
| 73 |  | 757,646,531 |  | 257,107,054 |  | 257,107,054 |  | - | 1,663,382 | - | 1,663,382 |
| 74 |  | 545,995,038 |  | 190,006,888 |  | 190,006,888 |  | - | 1,146,707 | - | 1,146,707 |
| 75 |  | 388,578,427 |  | 138,204,326 |  | 138,204,326 |  | - | 778,055 | - | 778,055 |
| 76 |  | 273,462,862 |  | 99,125,252 |  | 99,125,252 |  | - | 520,569 | - | 520,569 |
| 77 |  | 190,520,447 |  | 70,233,001 |  | 70,233,001 |  | - | 344,065 | - | 344,065 |
| 78 |  | 131,520,473 |  | 49,234,316 |  | 49,234,316 |  | - | 224,995 | - | 224,995 |
| 79 |  | 90,014,001 |  | 34,189,353 |  | 34,189,353 |  | - | 145,747 | - | 145,747 |
| 80 |  | 61,096,230 |  | 23,536,724 |  | 23,536,724 |  | - | 93,597 | - | 93,597 |
| 81 |  | 41,125,839 |  | 16,069,379 |  | 16,069,379 |  | - | 59,610 | - | 59,610 |
| 82 |  | 27,449,076 |  | 10,882,277 |  | 10,882,277 |  | - | 37,657 | - | 37,657 |
| 83 |  | 18,158,179 |  | 7,309,272 |  | 7,309,272 |  | - | 23,594 | - | 23,594 |
| 84 |  | 11,897,735 |  | 4,867,279 |  | 4,867,279 |  | - | 14,656 | - | 14,656 |
| 85 |  | 7,714,917 |  | 3,210,908 |  | 3,210,908 |  | - | 9,019 | - | 9,019 |
| 86 |  | 4,945,899 |  | 2,096,158 |  | 2,096,158 |  | - | 5,492 | - | 5,492 |
| 87 |  | 3,131,696 |  | 1,352,679 |  | 1,352,679 |  | - | 3,306 | - | 3,306 |
| 88 |  | 1,956,649 |  | 862,092 |  | 862,092 |  | - | 1,966 | - | 1,966 |
| 89 |  | 1,204,939 |  | 542,449 |  | 542,449 |  | - | 1,154 | - | 1,154 |
| 90 |  | 730,058 |  | 336,874 |  | 336,874 |  | - | 668 | - | 668 |
| 91 |  | 433,831 |  | 206,136 |  | 206,136 |  | - | 382 | - | 382 |
| 92 |  | 251,639 |  | 124,034 |  | 124,034 |  | - | 214 | - | 214 |
| 93 |  | 141,335 |  | 73,031 |  | 73,031 |  | - | 118 | - | 118 |
| 94 |  | 75,897 |  | 41,606 |  | 41,606 |  | - | 63 | - | 63 |
| 95 |  | 38,283 |  | 22,456 |  | 22,456 |  | - | 31 | - | 31 |
| 96 |  | 17,790 |  | 11,125 |  | 11,125 |  | - | 15 | - | 15 |
| 97 |  | 7,552 |  | 4,918 |  | 4,918 |  | - | 6 | - | 6 |
| 98 |  | 3,004 |  | 1,981 |  | 1,981 |  | - | 2 | - | 2 |
| 99 |  | 1,168 |  | 807 |  | 807 |  | - | 1 | - | 1 |
| 100 |  | 417 |  | 432 |  | 417 |  | - | 0 | - | 0 |
|  |  |  |  |  |  |  |  | Totals | \$ 107,108,329,044 | \$ - | \$ 107,108,329,044 |



## SECTION F

SUMMARY OF ASSUMPTIONS

# Summary of Assumptions Used to Develop Total Pension Liability Assumptions Adopted by ETF Board After CONSULTING WITH ACTUARY 

## Economic Assumptions

For determining plan liabilities, the discount rate is $5.0 \%$ for retired participants, $5.0 \%$ for active and inactive participants following retirement, and $7.2 \%$ for active participants prior to their retirement. A valuation performed assuming $5.5 \%$ discount rate for all participants at all stages of life, approximately reproduces the results of an actuarial valuation using the $5 \%$ post-retirement and $7.2 \%$ pre-retirement assumptions. Thus, it can be said that the net discount rate assumed in the valuations was $5.5 \%$ per year, compounded annually (net after administrative expenses).

The Wage Inflation Rate assumed in this valuation was $3.20 \%$ per year. The wage inflation rate is defined to be the portion of total pay increases for an individual that are due to macro economic forces including productivity, price inflation, and labor market conditions. The wage inflation rate does not include pay changes rated to individual merit and seniority effects.

No specific Price Inflation assumption is required to perform this valuation, since there are no benefits that are linked to price increases. However, a price inflation assumption on the order of $2.0 \%$ to $2.7 \%$ would be consistent with the other economic assumptions.

The assumed Real Rate of Return over wage inflation is defined to be the portion of total investment return that is more than the assumed total wage growth rate. Considering other economic assumptions, the $7.2 \%$ pre-retirement investment return rate translates to an assumed real rate of return over wage inflation of $4.0 \%$. The assumed real rate of return over price inflation would be higher - on the order of $4.5 \%$ to $5.2 \%$, considering both an inflation assumption and an average expense provision.

Pay increase assumptions for individual active members are shown for sample services below. Part of the assumption for each age is for merit and/or seniority increase, and the other $3.2 \%$ recognizes wage inflation, including price inflation, productivity increases, and other macro economic forces.

| \% Merit and Longevity Increase Next Year |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | University <br> Service | Gen. | Public School | Protective |  |
| Teachers | Teachers | With S.S. | w/o S.S. | Elec. |  |  |
|  |  |  |  |  |  |  |
| 1 | $3.5 \%$ | $3.2 \%$ | $5.8 \%$ | $4.8 \%$ | $5.5 \%$ | $2.0 \%$ |
| 2 | $3.5 \%$ | $3.2 \%$ | $5.8 \%$ | $4.8 \%$ | $5.5 \%$ | $2.0 \%$ |
| 3 | $3.1 \%$ | $3.1 \%$ | $5.4 \%$ | $4.1 \%$ | $4.7 \%$ | $2.0 \%$ |
| 4 | $2.8 \%$ | $3.0 \%$ | $5.1 \%$ | $3.5 \%$ | $3.8 \%$ | $1.9 \%$ |
| 5 | $2.5 \%$ | $2.9 \%$ | $4.7 \%$ | $2.8 \%$ | $3.0 \%$ | $1.9 \%$ |
|  |  |  |  |  |  |  |
| 10 | $1.5 \%$ | $2.4 \%$ | $3.2 \%$ | $1.1 \%$ | $0.9 \%$ | $1.6 \%$ |
| 15 | $1.1 \%$ | $1.7 \%$ | $1.8 \%$ | $0.8 \%$ | $0.5 \%$ | $1.2 \%$ |
| 20 | $0.9 \%$ | $1.1 \%$ | $0.8 \%$ | $0.7 \%$ | $0.4 \%$ | $0.7 \%$ |
| 25 | $0.6 \%$ | $0.8 \%$ | $0.4 \%$ | $0.6 \%$ | $0.3 \%$ | $0.4 \%$ |
| 30 | $0.4 \%$ | $0.6 \%$ | $0.2 \%$ | $0.5 \%$ | $0.2 \%$ | $0.3 \%$ |

## Decrement Probabilities

The mortality table used to measure mortality for retired participants was the Wisconsin 2012 Mortality Table, as adopted by the Board in connection with the 2009-2011 Experience Study. The rates in this table were based on actual WRS experience projected to 2017 with scale BB to allow for future improvements (margin) in mortality. Sample retirement values from this table are shown below. This assumption is used to measure the probabilities of participants dying before retirement and the probabilities of each benefit payment being made after retirement.

> Single Life Retirement Values
> Wisconsin 2012 Mortality Table with 5\% Interest

| Sample <br> Attained <br> Ages | Present Value of \$1 <br> Monthly for Life |  | Future Life <br> Expectancy (years) |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Males | Females | Males | Females |
| 40 | $\$ 209.20$ | $\$ 214.70$ | 42.9 | 46.1 |
| 45 | 200.43 | 207.06 | 38.1 | 41.3 |
| 50 | 189.60 | 197.69 | 33.3 | 36.5 |
| 55 | 176.75 | 186.37 | 28.7 | 31.8 |
| 60 | 162.35 | 172.92 | 24.4 | 27.2 |
| 65 | 145.13 | 156.75 | 20.1 | 22.7 |
| 70 | 125.71 | 137.76 | 16.1 | 18.4 |
| 75 | 104.34 | 116.43 | 12.4 | 14.3 |
| 80 | 82.05 | 93.57 | 9.0 | 10.7 |
| 85 | 61.28 | 70.89 | 6.3 | 7.6 |

The values shown above are for non-disabled participants. For disabled participants, the following table was used:

| Sample <br> Attained <br> Ages | Present Value of \$1 <br> Monthly for Life |  | Future Life <br> Expectancy (years) |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Males | Females | Males | Females |
| 40 | $\$ 195.27$ | $\$ 204.53$ | 35.7 | 39.9 |
| 45 | 183.23 | 194.56 | 30.9 | 35.1 |
| 50 | 169.52 | 182.61 | 26.4 | 30.4 |
| 55 | 153.66 | 168.39 | 22.1 | 25.8 |
| 60 | 135.14 | 151.44 | 18.0 | 21.4 |
| 65 | 114.76 | 131.73 | 14.1 | 17.2 |
| 70 | 92.83 | 109.91 | 10.6 | 13.2 |
| 75 | 71.03 | 86.92 | 7.6 | 9.7 |
| 80 | 52.06 | 64.92 | 5.2 | 6.8 |
| 85 | 36.73 | 47.23 | 3.5 | 4.7 |

## Active Participant Mortality Rates

| Sample <br> Attained Ages | Mortality Rates |  |
| :---: | :---: | :---: |
|  | Males | Females |
|  |  |  |
| 20 | 0.000155 | 0.000089 |
| 25 | 0.000184 | 0.000097 |
| 30 | 0.000229 | 0.000129 |
| 35 | 0.000398 | 0.000230 |
|  |  |  |
| 40 | 0.000540 | 0.000329 |
| 45 | 0.000717 | 0.000519 |
| 50 | 0.000966 | 0.000765 |
| 55 | 0.002228 | 0.001345 |
|  |  |  |
| 60 | 0.003147 | 0.001935 |
| 65 | 0.004814 | 0.002974 |
| 70 | 0.007979 | 0.005057 |
| 75 | 0.013576 | 0.009155 |
| 80 | 0.024949 | 0.017103 |

This assumption is used to measure the probability of participants dying while in service.

## Rates of Retirement for Those Eligible To Retire

Normal Retirement

| Age | General |  | Public School |  | University |  | Protective* |  | Exec. \& Elected |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Male | Female | Male | Female | Male | Female | With S.S. | W/O S.S. |  |
| 50 |  |  |  |  |  |  | 6\% | $4 \%$ |  |
| 51 |  |  |  |  |  |  | 7\% | 4\% |  |
| 52 |  |  |  |  |  |  | 8\% | 5\% |  |
| 53 |  |  |  |  |  |  | 23\% | 17\% |  |
| 54 |  |  |  |  |  |  | 18\% | 25\% |  |
| 55 |  |  |  |  |  |  | 17\% | 21\% |  |
| 56 |  |  |  |  |  |  | 16\% | 27\% |  |
| 57 | 20\% | 17\% | 40\% | 27\% | 13\% | 14\% | 16\% | 30\% | 15\% |
| 58 | 20\% | 17\% | 35\% | 27\% | 13\% | 14\% | 16\% | 30\% | 15\% |
| 59 | 20\% | 17\% | 25\% | 27\% | 13\% | 13\% | 16\% | 30\% | 15\% |
| 60 | 20\% | 20\% | 28\% | 27\% | 13\% | 13\% | 18\% | 26\% | 10\% |
| 61 | 20\% | 20\% | 25\% | 27\% | 13\% | 19\% | 18\% | 15\% | 13\% |
| 62 | 27\% | 27\% | 36\% | $34 \%$ | 15\% | 19\% | 22\% | 20\% | 13\% |
| 63 | 32\% | 28\% | 32\% | 27\% | 15\% | 19\% | 29\% | 40\% | 12\% |
| 64 | 24\% | 25\% | 24\% | 23\% | 15\% | 18\% | 16\% | 40\% | 12\% |
| 65 | 24\% | 25\% | 24\% | 28\% | 15\% | 22\% | 30\% | 40\% | 12\% |
| 66 | 30\% | 29\% | 25\% | 30\% | 20\% | 23\% | 20\% | 40\% | 20\% |
| 67 | 24\% | 20\% | 24\% | 28\% | 18\% | 17\% | 15\% | 40\% | 17\% |
| 68 | 17\% | 18\% | 24\% | 26\% | 18\% | 17\% | 25\% | 40\% | 15\% |
| 69 | 17\% | 18\% | 24\% | 20\% | 18\% | 17\% | 20\% | 40\% | 15\% |
| 70 | 17\% | 18\% | 20\% | 20\% | 20\% | 20\% | 100\% | 100\% | 13\% |
| 71 | 17\% | 18\% | 20\% | 20\% | 20\% | 20\% | 100\% | 100\% | 13\% |
| 72 | 17\% | 15\% | 20\% | 20\% | 15\% | 20\% | 100\% | 100\% | 25\% |
| 73 | 17\% | 15\% | 20\% | 20\% | 15\% | 20\% | 100\% | 100\% | 10\% |
| 74 | 17\% | 15\% | 20\% | 20\% | 15\% | 20\% | 100\% | 100\% | 10\% |
| 75 | 100\% | 100\% | 100\% | 100\% | 100\% | 100\% | 100\% | 100\% | 100\% |

* Includes early retirements.

Early Retirement

| Age | \% Retiring Next Year |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | General |  | Public School |  | University |  | Exec. \& Elected |
|  | Male | Female | Male | Female | Male | Female |  |
| 55 | 8.0\% | 6.1\% | 12.0\% | 11.0\% | 4.8\% | 5.5\% | 4.5\% |
| 56 | 8.0\% | 6.4\% | 12.0\% | 11.0\% | 3.0\% | 5.5\% | 4.5\% |
| 57 | 4.3\% | 4.2\% | 12.0\% | 11.0\% | 2.0\% | 4.0\% | 4.5\% |
| 58 | 5.3\% | 5.5\% | 12.0\% | 11.0\% | 2.5\% | 4.0\% | 4.5\% |
| 59 | 5.5\% | 5.3\% | 12.0\% | 11.0\% | 4.0\% | 6.5\% | 4.5\% |
| 60 | 7.5\% | 8.1\% | 12.0\% | 15.0\% | 4.0\% | 6.5\% | 4.5\% |
| 61 | 8.0\% | 7.0\% | 12.0\% | 15.0\% | 7.5\% | 7.5\% | 4.5\% |
| 62 | 14.0\% | 15.0\% | 20.0\% | 20.0\% | 7.0\% | 10.0\% |  |
| 63 | 16.0\% | 15.0\% | 20.0\% | 20.0\% | 7.5\% | 10.0\% |  |
| 64 | 17.0\% | 15.0\% | 20.0\% | 20.0\% | 8.0\% | 13.0\% |  |

The assumed rates of separation from employment prior to service retirement due to disability and other causes are shown below for sample ages. For other terminations it was assumed that a percentage depending on age of participants terminating after age 35 with 5 or more years service will leave their contributions on deposit and be paid a benefit at normal retirement age and that the remaining participants would take a separation benefit. The percentage taking a separation benefit is $25 \%$ at age 35 , grading downward to $0 \%$ at retirement eligibility. All participants terminating prior to normal retirement age with less than 5 years of service were assumed to take a separation benefit.

## Assumed Termination Rates <br> by Attained Age and Years of Service

| Age | Service | \% of Active Participants Terminating |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Protective |  | Public Schools |  | University |  |  <br> Elected | General |  |
|  |  | With <br> Soc. <br> Sec. | Without Soc. Sec. |  |  |  |  |  |  |  |
|  |  |  |  | Males | Females | Males | Females |  | Males | Females |
|  | 0 | 15.0\% | 4.0\% | 17.7\% | 15.0\% | 18.3\% | 22.0\% | 20.0\% | 17.5\% | 19.5\% |
|  | 1 | 7.0\% | 3.5\% | 11.4\% | 10.5\% | 15.0\% | 15.0\% | 14.0\% | 13.0\% | 13.5\% |
|  | 2 | 4.3\% | 2.1\% | 7.3\% | 7.1\% | 11.3\% | 12.5\% | 14.0\% | 8.5\% | 10.0\% |
|  | 3 | 3.8\% | 1.3\% | 5.2\% | 5.5\% | 9.6\% | 10.0\% | 10.0\% | 6.8\% | 8.0\% |
|  | 4 | 3.4\% | 1.2\% | 3.9\% | 4.6\% | 8.5\% | 9.5\% | 10.0\% | 6.0\% | 7.4\% |
|  | 5 | 2.6\% | 1.1\% | 3.0\% | 4.0\% | 7.5\% | 8.0\% | 9.0\% | 4.5\% | 6.0\% |
|  | 6 | 2.5\% | 1.0\% | 2.8\% | 3.5\% | 7.0\% | 7.0\% | 8.5\% | 4.0\% | 5.0\% |
|  | 7 | 2.3\% | 0.9\% | 2.5\% | 3.0\% | 5.5\% | 6.0\% | 8.0\% | 3.5\% | 4.5\% |
|  | 8 | 2.0\% | 0.8\% | 2.0\% | 2.5\% | 4.3\% | 5.0\% | 7.5\% | 3.0\% | 4.0\% |
|  | 9 | 1.7\% | 0.7\% | 1.8\% | 2.3\% | 3.2\% | 4.0\% | 7.0\% | 2.5\% | 3.8\% |
| 25 | 10 \& Over | 1.7\% | 0.7\% | 1.8\% | 2.2\% | 3.2\% | 5.0\% | 6.0\% | 2.5\% | 3.8\% |
| 30 |  | 1.6\% | 0.7\% | 1.4\% | 1.9\% | 3.2\% | 4.5\% | 5.1\% | 2.5\% | 3.3\% |
| 35 |  | 1.4\% | 0.7\% | 1.2\% | 1.4\% | 3.1\% | 4.0\% | 4.2\% | 2.1\% | 2.8\% |
| 40 |  | 1.2\% | 0.6\% | 1.1\% | 1.1\% | 2.7\% | 3.4\% | 3.7\% | 1.6\% | 2.2\% |
| 45 |  | 1.1\% | 0.6\% | 1.0\% | 0.9\% | 2.1\% | 2.6\% | 3.3\% | 1.3\% | 1.8\% |
| 50 |  | 1.0\% | 0.5\% | 1.0\% | 0.9\% | 1.6\% | 1.8\% | $3.1 \%$ | 1.1\% | 1.6\% |
| 55 |  | 1.0\% | 0.5\% | 1.0\% | 0.9\% | 1.4\% | 1.5\% | 3.0\% | 1.1\% | 1.5\% |
| 60 |  | 1.0\% | 0.5\% | 1.0\% | 0.9\% | 1.4\% | 1.5\% | 3.0\% | 1.1\% | 1.5\% |

## Disability Rates

| Age | \% of Active Participants Becoming Disabled |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Protective |  | Public Schools |  | University |  | Exec. \& Elected |  | General |  |
|  | With SS | W/O SS | Males | Females | Males | Females | Males | Females | Males | Females |
| 20 | $0.01 \%$ | $0.04 \%$ | $0.01 \%$ | $0.01 \%$ | $0.01 \%$ | $0.01 \%$ | $0.00 \%$ | $0.00 \%$ | $0.01 \%$ | $0.01 \%$ |
| 25 | $0.01 \%$ | $0.04 \%$ | $0.01 \%$ | $0.01 \%$ | $0.01 \%$ | $0.01 \%$ | $0.00 \%$ | $0.00 \%$ | $0.01 \%$ | $0.01 \%$ |
| 30 | $0.01 \%$ | $0.04 \%$ | $0.01 \%$ | $0.01 \%$ | $0.01 \%$ | $0.01 \%$ | $0.00 \%$ | $0.00 \%$ | $0.01 \%$ | $0.03 \%$ |
| 35 | $0.02 \%$ | $0.04 \%$ | $0.01 \%$ | $0.01 \%$ | $0.01 \%$ | $0.03 \%$ | $0.01 \%$ | $0.01 \%$ | $0.01 \%$ | $0.04 \%$ |
| 40 | $0.03 \%$ | $0.07 \%$ | $0.02 \%$ | $0.02 \%$ | $0.01 \%$ | $0.04 \%$ | $0.01 \%$ | $0.01 \%$ | $0.04 \%$ | $0.05 \%$ |
| 45 | $0.05 \%$ | $0.13 \%$ | $0.04 \%$ | $0.06 \%$ | $0.02 \%$ | $0.04 \%$ | $0.01 \%$ | $0.01 \%$ | $0.07 \%$ | $0.07 \%$ |
| 50 | $0.08 \%$ | $0.74 \%$ | $0.11 \%$ | $0.12 \%$ | $0.04 \%$ | $0.07 \%$ | $0.02 \%$ | $0.02 \%$ | $0.15 \%$ | $0.11 \%$ |
| 55 | $1.21 \%$ | $0.54 \%$ | $0.21 \%$ | $0.17 \%$ | $0.11 \%$ | $0.10 \%$ | $0.09 \%$ | $0.09 \%$ | $0.29 \%$ | $0.20 \%$ |
| 60 | $2.04 \%$ | $0.16 \%$ | $0.34 \%$ | $0.25 \%$ | $0.14 \%$ | $0.15 \%$ | $0.11 \%$ | $0.11 \%$ | $0.51 \%$ | $0.29 \%$ |

## SECTION G <br> PLAN PROVISIONS

## Summary of Benefit Provisions

## Normal Retirement Eligibility

The age a participant becomes eligible for an unreduced age and service annuity is:

| General |  | Protective |  | Executive \& Elected |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Age | Service | Age | Service | Age | Service |
|  |  |  |  |  |  |
| 65 | Any* | 54 | Any* | 62 | Any* |
| 57 | 30 | 53 | 25 | 57 | 30 |

* Participants first employed after 1989 and terminated before April 24, 1998 must have
creditable service in 5 calendar years. creditable service in 5 calendar years.


## Normal Retirement Annuity

The age and service annuity payable at Normal Retirement Age is based on Final Average Earnings (FAE) and Creditable Service (CS) as follows:

| Multiplier for Service Rendered |  |  |  |
| :---: | :---: | :---: | :---: |
| Before <br> $\mathbf{2 0 0 0}$ | Between 2000 <br> and 2011 | After <br> $\mathbf{2 0 1 1}$ |  |
| $2.165 \%$ | $2.0 \%$ | $1.6 \%$ | Executive group and elected officials |
| $2.165 \%$ | $2.0 \%$ | $2.0 \%$ | Protective occupation participants covered by Social Security |
| $2.665 \%$ | $2.5 \%$ | $2.5 \%$ | Protective occupation participants not covered by Social Security |
| $1.765 \%$ | $1.6 \%$ | $1.6 \%$ | All other participants |

FAE is generally the average of the 3 highest years of earnings (July 1 - June 30 for teachers, educational support staff, and judges; calendar year for others) preceding retirement. These years do not have to be consecutive. For legislators and state constitutional officers who are ineligible to receive pay increases during their term, FAE is the statutory rate of earnings at termination.

Maximum formula annuity is $85 \%$ of FAE for protective occupation participants not covered by Social Security, $65 \%$ of FAE for protectives covered by Social Security, and $70 \%$ for all other participants. If greater than the formula amount, an annuity equal to the actuarial equivalent of two times the required accumulated contributions is paid in lieu of the formula amount.

Early Retirement. Any participant who has attained age 55 and any Protective occupation participant who has attained age 50 may apply for an early retirement annuity. The benefit is reduced $0.4 \%$ for each month that the annuity effective date precedes the Normal Retirement Age. For NonProtective participants terminating after $6 / 30 / 90$, the $0.4 \%$ is reduced for months after the attainment of age 57 and before the annuity effective date by $.001111 \%$ for each month of creditable service.

Voluntary Termination Before Immediate Benefit Eligibility. Participant may either (i) receive a refund of accumulated contributions, or (ii) leave contributions on deposit and apply for a retirement annuity on or after the minimum retirement age based upon age and accrued service at time of termination.

Post-Retirement Adjustments. Annuities are increased annually if the investment income credited to retired life funds is in excess of the assumed benefit rate (presently 5\%), other plan experiences are within projected ranges, and the resulting adjustment would be at least $0.5 \%$.

Disability Annuity. Eligibility: generally total and permanent incapacity to engage in gainful employment. Participant must have completed at least 6 months of creditable service (in at least 5 out of the last 7 calendar years) preceding application for disability. Service requirement is waived if disability is from service-related causes.

For protective occupations, eligibility also can be met if a member has 15 years of service, is between the ages of 50 and 55 and unable to safely and efficiently perform one's duties.

Disability Amounts. Amounts payable in case of disability depend upon the plan from which payment is made and are described below.

|  | Pre-10/16/92 WRS Plan | Post-10/15/92 LTDI Plan |
| :--- | :--- | :--- |
| Participants covered | Participants hired before 10/16/92 who <br> do not elect LTDI coverage. | Participants entering after 10/15/92 and <br> participants on 10/15/92 who elect <br> LTDI coverage. |
| Benefit to age 65* | WRS formula benefit based on service <br> projected to normal retirement age. | $40 \%$ of FAE for participants covered by <br> Social Security; 50\% of FAE for non- <br> covered participants who cannot qualify <br> for Social Security disability benefits. |
| Benefit at age 65* | Continuation of pre-65 amount. | WRS benefit accrued to date of <br> disability plus 7\% of FAE money <br> purchase benefit during disability <br> period, both of which are adjusted in <br> accordance with dividend rate. |

* Conversion age is later for participants becoming disabled after age 61.


## Death-in-Service.

(a) Prior to age 50 for Protective participants, age 55 for others, the benefit is the equivalent of twice the accumulated employee contributions required and all additional contributions and employer amounts contributed prior to 1974 for teachers, or 1966 for others.
(b) After age 50 for Protective participants, age 55 for others, the benefit is the amount that would have been paid if participant had retired and elected $100 \%$ survivor option. Benefit is payable to any natural living person.

Interest Credits. For years after 1999, and for people with some active service after 1999, participant core accounts (including the variable at core accounts) are credited with interest at the full (core) effective rate. For others, accounts are credited with interest as follows:

|  | Rate Credited For Purpose of |  |  |
| :--- | :---: | :---: | :---: |
| Date of Participation | Money Purchase <br> Minimum | Refunds |  |
| Prior to 1982 | Actual | Actual |  |
| January $1,1982 \&$ Later | $5 \%$ | $3 \%$ |  |

Participant variable accounts are credited with interest based on the earnings in the variable portfolio.

Contribution Rates. The financial objective of WRS is to establish and receive contributions that will remain level from year to year and decade to decade.

Statutory required participant contributions prior to July 1, 2011 were as follows:

| General | $5.0 \%$ |
| :--- | :--- |
| Executives \& Elected <br> $\quad$ Officials | 5.5 |
| Protectives |  |
| $\quad$ - With Social Security | 6.0 |
| $\quad$ - Without Social Security | 8.0 |

Statutory required participant contributions after July 1, 2011 are set equal to one-half of the actuarially determined rate for General participants and Executive and Elected Officials. Participant contributions for Protective participants are set equal to the participant contribution for General members.

Normal Form of Benefit. The normal form of benefit is a straight life annuity with no death benefits. Optional forms of benefit which are actuarially reduced are listed below:

- A life annuity with 60 or 180 monthly payments guaranteed.
- A joint survivorship annuity with $75 \%$ continued to beneficiary.
- A joint survivorship annuity with $100 \%$ continued to beneficiary.
- A joint survivorship annuity reduced $25 \%$ upon either your death or your beneficiary's death.
- A joint survivorship annuity with $100 \%$ continued to beneficiary combined with 180 monthly payments guaranteed.

For formula benefit calculations, optional forms are calculated at the lower of the current age or age 62 (Normal Retirement Age for Protective occupations).

Vesting. Participants hired prior to July 1, 2011 vest immediately. After July 1, 2011, participants vest after 5 years of service.

## SECTION H

GLOSSARY OF TERMS

## Glossary of Terms

Actuarial Accrued Liability (AAL)

Actuarial Assumptions

Accrued Service

Actuarial Equivalent

## Actuarial Cost Method

## Actuarial Gain (Loss)

## Actuarial Present Value (APV)

## Actuarial Valuation

## Actuarial Valuation Date

Actuarially Determined
Contribution (ADC) or
Annual Required
Contribution (ARC)

The AAL is the difference between the actuarial present value of all benefits and the actuarial value of future normal costs. The definition comes from the fundamental equation of funding which states that the present value of all benefits is the sum of the Actuarial Accrued Liability and the present value of future normal costs. The AAL may also be referred to as "accrued liability" or "actuarial liability."

These assumptions are estimates of future experience with respect to rates of mortality, disability, turnover, retirement, rate or rates of investment income and compensation increases. Actuarial assumptions are generally based on past experience, often modified for projected changes in conditions. Economic assumptions (compensation increases, payroll growth, inflation and investment return) consist of an underlying real rate of return plus an assumption for a long-term average rate of inflation.

Service credited under the system which was rendered before the date of the actuarial valuation.

A single amount or series of amounts of equal actuarial value to another single amount or series of amounts, computed on the basis of appropriate actuarial assumptions.

A mathematical budgeting procedure for allocating the dollar amount of the actuarial present value of the pension trust benefits between future normal cost and actuarial accrued liability. The actuarial cost method may also be referred to as the actuarial funding method.

The difference in liabilities between actual experience and expected experience during the period between two actuarial valuations is the gain (loss) on the accrued liabilities.

The amount of funds currently required to provide a payment or series of payments in the future. The present value is determined by discounting future payments at predetermined rates of interest and probabilities of payment.

The actuarial valuation report determines, as of the actuarial valuation date, the service cost, total pension liability, and related actuarial present value of projected benefit payments for pensions.

The date as of which an actuarial valuation is performed.
A calculated contribution into a defined benefit pension plan for the reporting period, most often determined based on the funding policy of the plan. Typically the Actuarially Determined Contribution has a normal cost payment and an amortization payment.

## Glossary of Terms

## Amortization Payment

Amortization Method

Cost-of-Living Adjustments

Cost-Sharing Multiple-<br>Employer Defined Benefit<br>Pension Plan (cost-sharing pension plan)<br>Covered-Employee Payroll

## Deferred Retirement Option Program (DROP)

The amortization payment is the periodic payment required to pay off an interest-discounted amount with payments of interest and principal.

The method used to determine the periodic amortization payment may be a level dollar amount, or a level percent of pay amount. The period will typically be expressed in years, and the method will either be "open" (meaning, reset each year) or "closed" (the number of years remaining will decline each year.

Postemployment benefit changes intended to adjust benefit payments for the effects of inflation.

A multiple-employer defined benefit pension plan in which the pension obligations to the employees of more than one employer are pooled and pension plan assets can be used to pay the benefits of the employees of any employer that provides pensions through the pension plan.

The payroll of covered employees, which is typically only the pensionable pay and does not include pay above any pay cap.

A program that permits a plan member to elect a calculation of benefit payments based on service credits and salary, as applicable, as of the DROP entry date. The plan member continues to provide service to the employer and is paid for the service by the employer after the DROP entry date; however, the pensions that would have been paid to the plan member are credited to an individual member account within the defined benefit pension plan until the end of the DROP period. Other variations for DROP exist and will be more fully detailed in the plan provision section of the valuation report.

The deferred inflows and outflows of pension resources are amounts used under GASB Statement No. 68 in developing the annual pension expense. Deferred inflows and outflows arise with differences between expected and actual experiences; changes of assumptions. The portion of these amounts not included in pension expense should be included in the deferred inflows or outflows of resources.

For GASB purposes, the discount rate is the single rate of return that results in the present value of all projected benefit payments to be equal to the sum of the funded and unfunded projected benefit payments, specifically:

1. The benefit payments to be made while the pension plans' fiduciary net position is projected to be greater than the benefit payments that are projected to be made in the period and;
2. The present value of the benefit payments not in (1) above, discounted using the municipal bond rate.

## Glossary of Terms

Entry Age Actuarial Cost Method (EAN)

Long-Term Expected Rate of Return

Money-Weighted Rate of
Return

## Multiple-Employer Defined Benefit Pension Plan

Municipal Bond Rate

Net Pension Liability (NPL)

Non-employer Contribution Entities

## Normal Cost

GASB The Governmental Accounting Standards Board is an organization that
The Governmental Accounting Standards Board is an organization that
exists in order to promulgate accounting standards for governmental entities.

The fiduciary net position is the value of the assets of the trust.
The EAN is a funding method for allocating the costs of the plan between the normal cost and the accrued liability. The actuarial present value of the projected benefits of each individual included in an actuarial valuation is allocated on a level basis (either level dollar or level percent of pay) over the earnings or service of the individual between entry age and assumed exit ages(s). The portion of the actuarial present value allocated to a valuation year is the normal cost. The portion of this actuarial present value not provided for at a valuation date by the actuarial present value of future normal costs is the actuarial accrued liability. The sum of the accrued liability plus the present value of all future normal costs is the present value of all benefits.

The long-term rate of return is the expected return to be earned over the entire trust portfolio based on the asset allocation of the portfolio.

The money-weighted rate of return is a method of calculating the
returns that adjusts for the changing amounts actually invested.
For purposes of GASB Statement No. 67, money-weighted rate of
return is calculated as the internal rate of return on pension plan
investments, net of pension plan investment expense.
A multiple-employer plan is a defined benefit pension plan that is used to provide pensions to the employees of more than one employer.

The Municipal Bond Rate is the discount rate to be used for those benefit payments that occur after the assets of the trust have been depleted.

The NPL is the liability of employers and non-employer contribution entities to plan members for benefits provided through a defined benefit pension plan.

Non-employer contribution entities are entities that make contributions to a pension plan that is used to provide pensions to the employees of other entities. For purposes of the GASB Accounting statement plan members are not considered non-employer contribution entities.

The actuarial present value of the pension trust benefits allocated to the current year by the actuarial cost method.

## Glossary of Terms

Other Postemployment Benefits (OPEB)

Real Rate of Return

Service Cost

Total Pension Expense

All postemployment benefits other than retirement income (such as death benefits, life insurance, disability, and long-term care) that are provided separately from a pension plan, as well as postemployment healthcare benefits regardless of the manner in which they are provided. Other postemployment benefits do not include termination benefits.

The real rate of return is the rate of return on an investment after adjustment to eliminate inflation.

The service cost is the portion of the actuarial present value of projected benefit payments that is attributed to a valuation year.

The total pension expense is the sum of the following items that are recognized at the end of the employer's fiscal year:

1. Service Cost
2. Interest on the Total Pension Liability
3. Current-Period Benefit Changes
4. Employee Contributions (made negative for addition here)
5. Projected Earnings on Plan Investments (made negative for addition here)
6. Pension Plan Administrative Expense
7. Other Changes in Plan Fiduciary Net Position
8. Recognition of Outflow (Inflow) of Resources due to Liabilities
9. Recognition of Outflow (Inflow) of Resources due to Assets

Total Pension Liability (TPL) The TPL is the portion of the actuarial present value of projected benefit payments that is attributed to past periods of member service.

The UAAL is the difference between actuarial accrued liability and valuation assets.

The valuation assets are the assets used in determining the unfunded liability of the plan. For purposes of the GASB Statement No. 67, the valuation asset is equal to the market value of assets.

